

# Fast algorithms of d-dimensional DFT of real signal in commutative-associative algebras

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## Abstract

The aim of this work is to develop fast algorithms for computing the so-called "hypercomplex" discrete Fourier transforms (DFT) and analyze their computational characteristics.

**Keywords:** d-dimensional DFT, commutative-associative algebra, fast algorithm, discrete Fourier transforms.

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